

Abstract: This study investigates the dynamic crushing behavior of multi-layered brass plates based on the Miura-Ori tessellation, focusing on the strategic implementation of graded stiffness to enhance Specific Energy Absorption (SEA). Using high-fidelity finite element analysis (Abaqus/Explicit) validated against experimental data, the research evaluates how varying sector angles (ϕ) across stacked layers influences deformation mechanisms under diverse loading rates. A comparative analysis between homogeneous and functionally graded configurations reveals that out-of-plane compression triggers a unique "self-locking" phenomenon in graded structures. Furthermore, the study explores the in-plane response, identifying a distinct auxetic behavior with negative Poisson's ratios (ν_{xy}) that persist under dynamic regimes. These findings suggest that origami-inspired gradations offer a programmable pathway for tailoring the impact response of next-generation aerospace and automotive components.

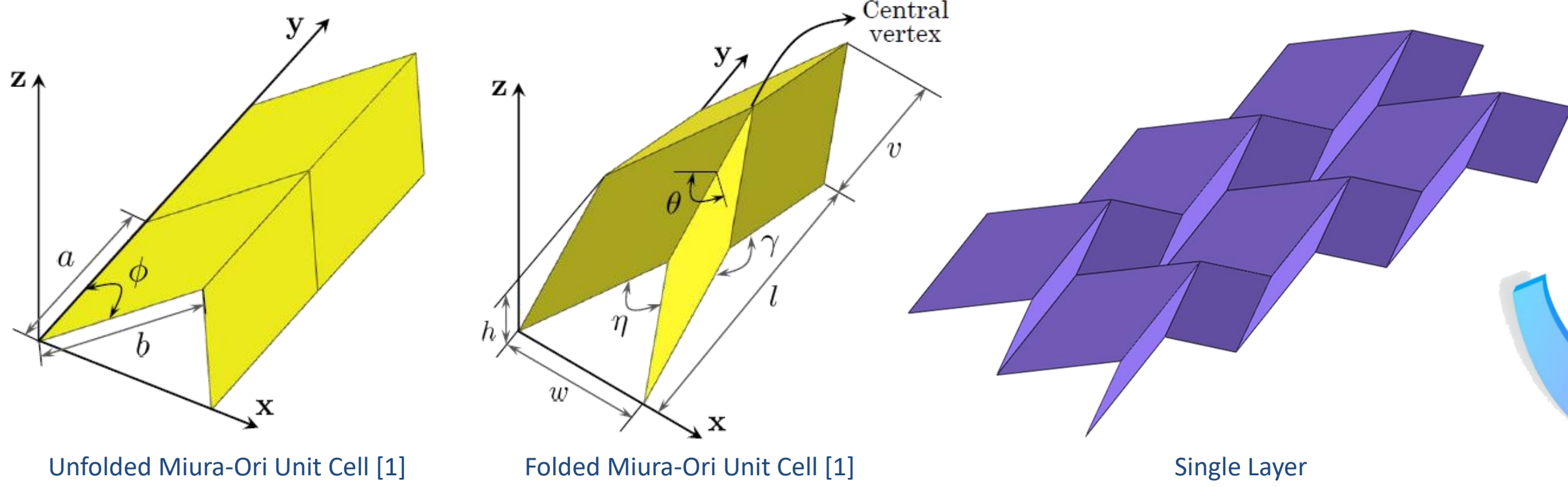
1. Description of the Problem

The problem analyzed consists on the uniaxial compression test of multi-layer Origami plates, in dynamic regime. The base geometry is the Miura-Ori unit cell, which can be defined using four independent geometrical parameters, which lead to six new geometrical entities defined by the following equations:

$$\cos \gamma = \frac{\sin^2 \phi \cos^2(\theta/2) - \cos^2 \phi}{\sin^2 \phi \cos^2(\theta/2) + \cos^2 \phi} \quad \cos \eta = \sin^2 \phi \cos \theta + \cos^2 \phi \quad w = 2b \cdot \sin(\eta/2) \quad l = 2a \cdot \sin(\gamma/2)$$

$$h = a \cdot \cos(\gamma/2) \quad v = b \cdot \cos(\eta/2)$$

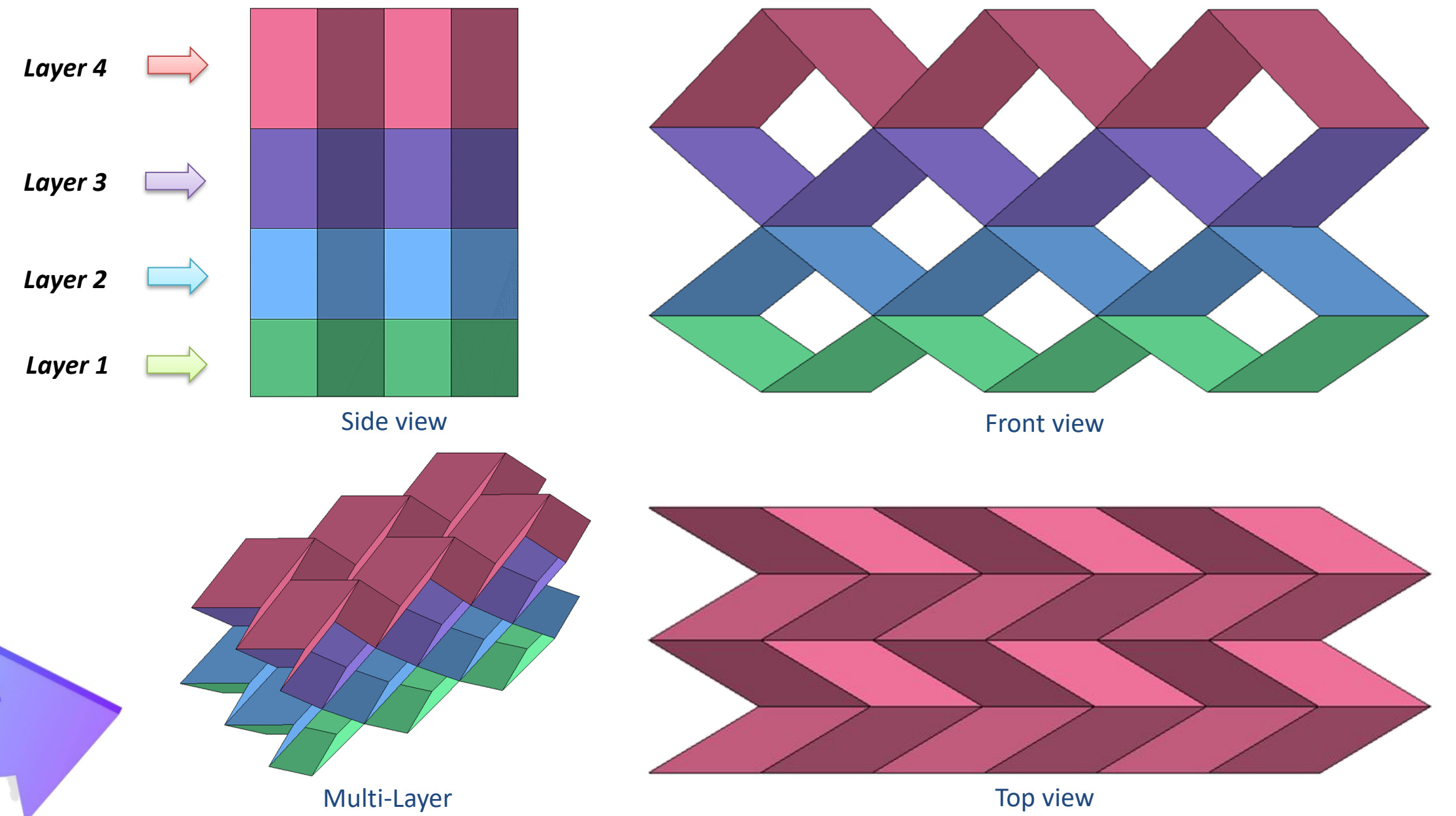
Geometrical parameters of the Miura-Ori unit cell



1.1. Configurations analyzed:

- Homogeneous structure: $\phi_1 = 48^\circ \quad \phi_2 = 48^\circ \quad \phi_3 = 48^\circ \quad \phi_4 = 48^\circ$
- Graded structure: $\phi_1 = 39^\circ \quad \phi_2 = 45^\circ \quad \phi_3 = 51^\circ \quad \phi_4 = 57^\circ$

1.2. Geometry of the graded structure: To create a 3D structure with geometric gradient, layers with different sector angles are stacked in the out-of-plane z direction. In this case, the geometrical parameters must fulfil some additional constraints



$$a_j = \frac{a_1 \cos \phi_1}{\cos \phi_j} \quad b_j = b_1 \quad \theta_j = \cos^{-1} \left(1 - \frac{2 \sin^2(\theta_1/2) \sin^2 \phi_1}{\sin^2 \phi_j} \right)$$

Geometrical constraints for the multi-layer structure

2. Material and Numerical Model

2.1. Material properties for Brass (CuZn40)

The material of the main structure has been considered has elastic-plastic with linear hardening equation [2].

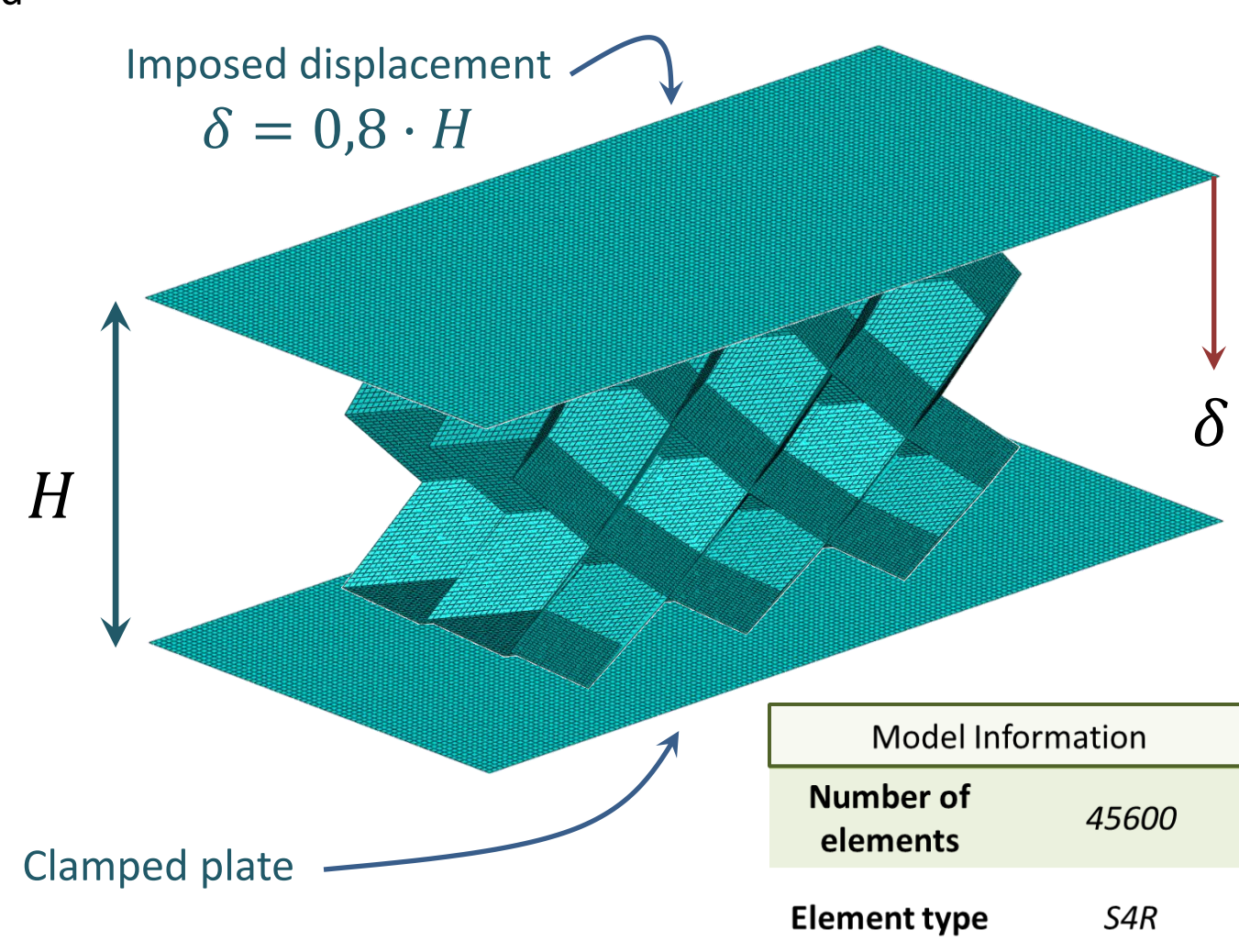
Density	$\rho = 8.33 \text{ g}\cdot\text{cm}^{-3}$
Elastic Modulus	$E = 111.1 \text{ GPa}$
Poisson coefficient	$\nu = 0.346$
Yield stress	$\sigma_y = 142 \text{ MPa}$
Tensile strength	$\sigma_u = 424.9 \text{ MPa}$
Elongation	$\epsilon_u = 0.242$

2.2. Material properties for steel: Material considered for the compressive plates.

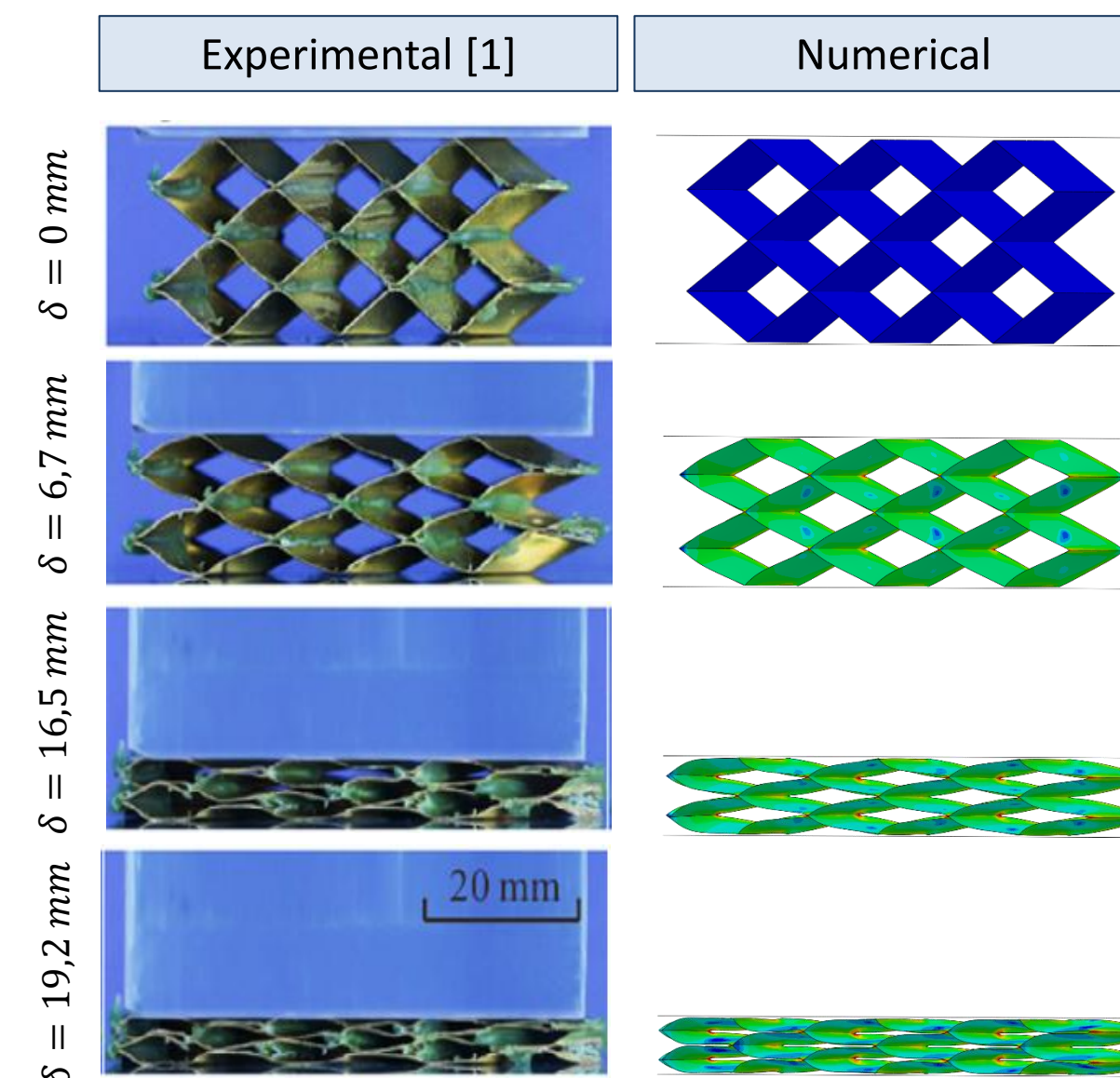
Density	$\rho = 7.85 \text{ g}\cdot\text{cm}^{-3}$
Elastic Modulus	$E = 210.0 \text{ GPa}$

2.3. Numerical model

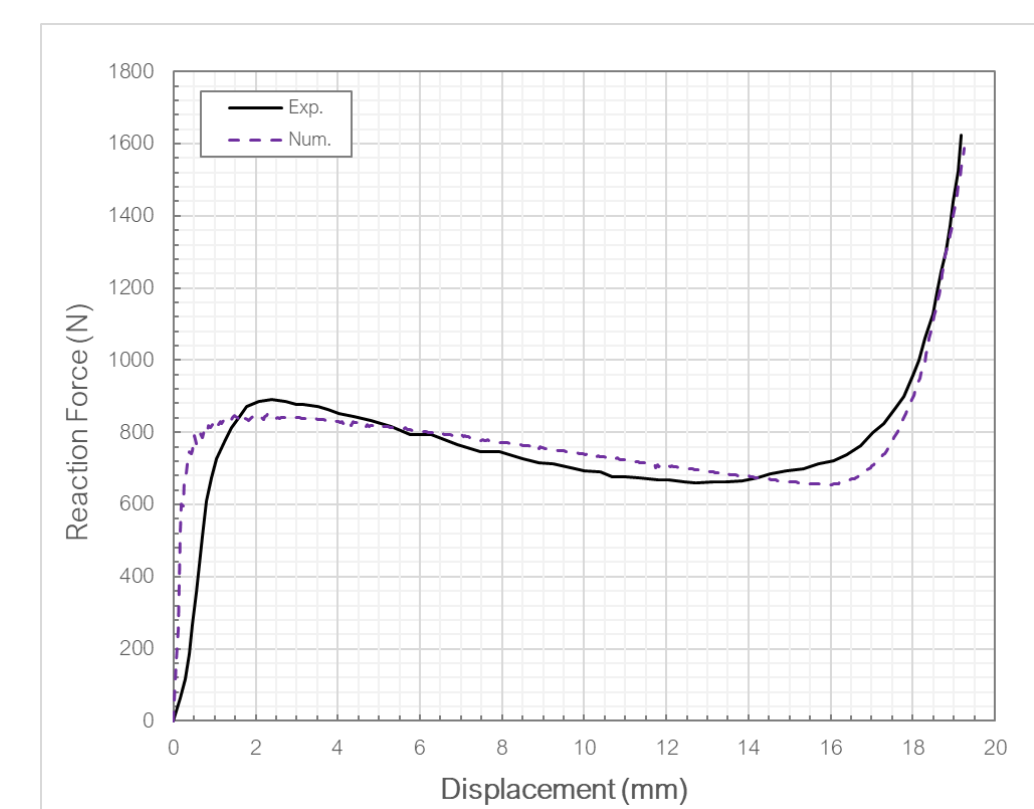
All the components, the two plates and the multi-layer origami structure, are defined as shell geometries



3. Validation



The relative error in terms of absorbed energy is **3.28 %**



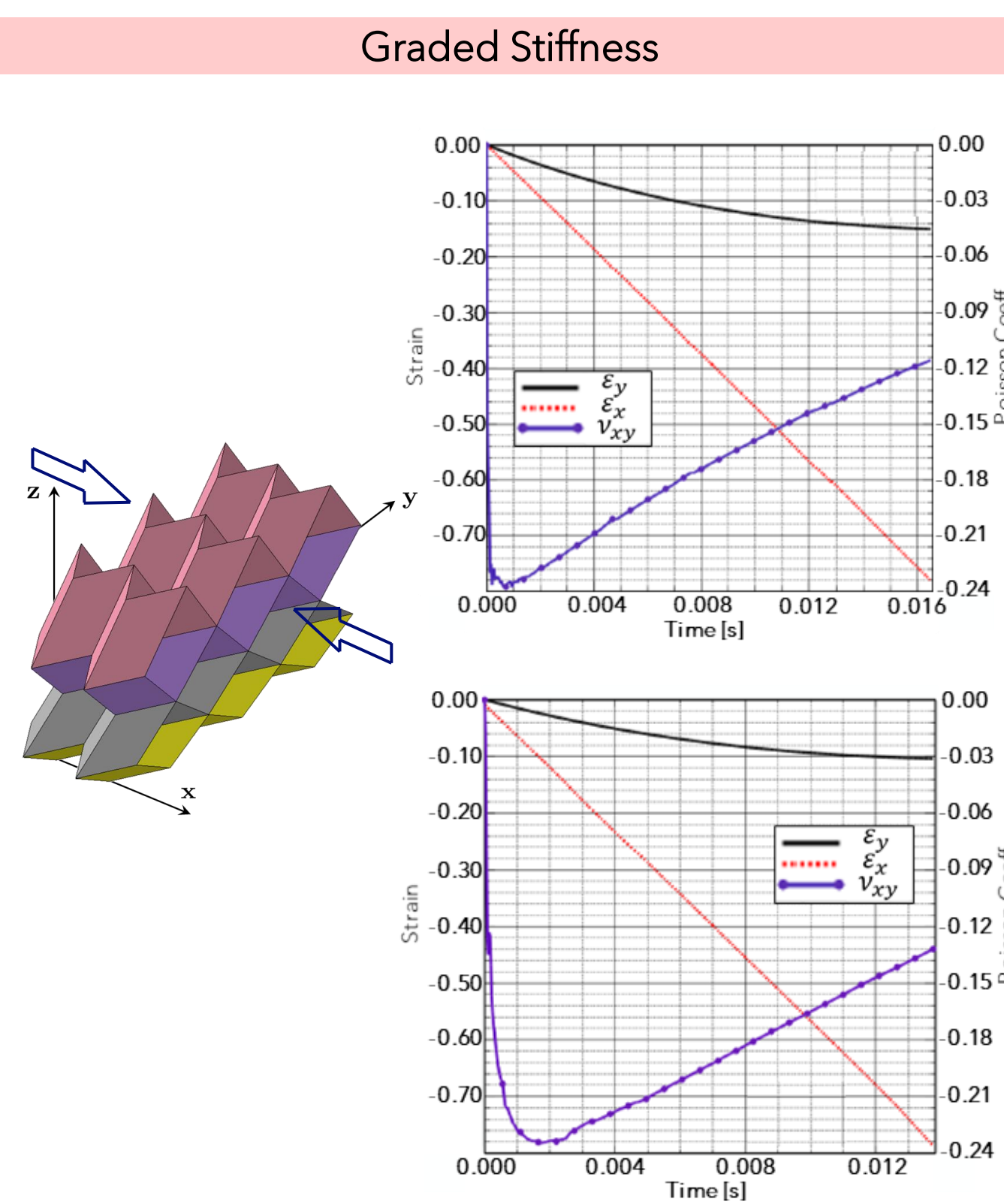
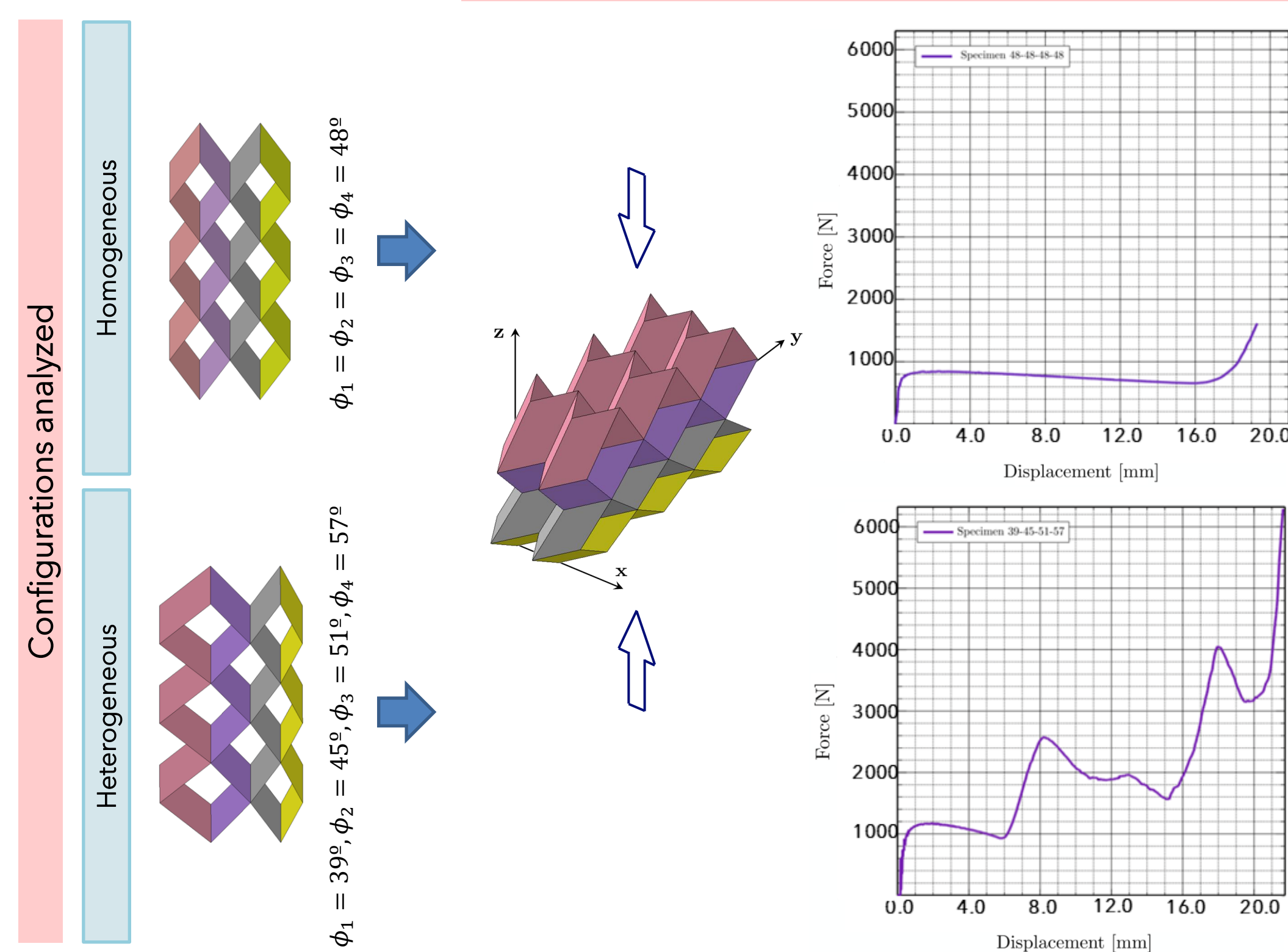
MODEL VALIDATED

4. Results

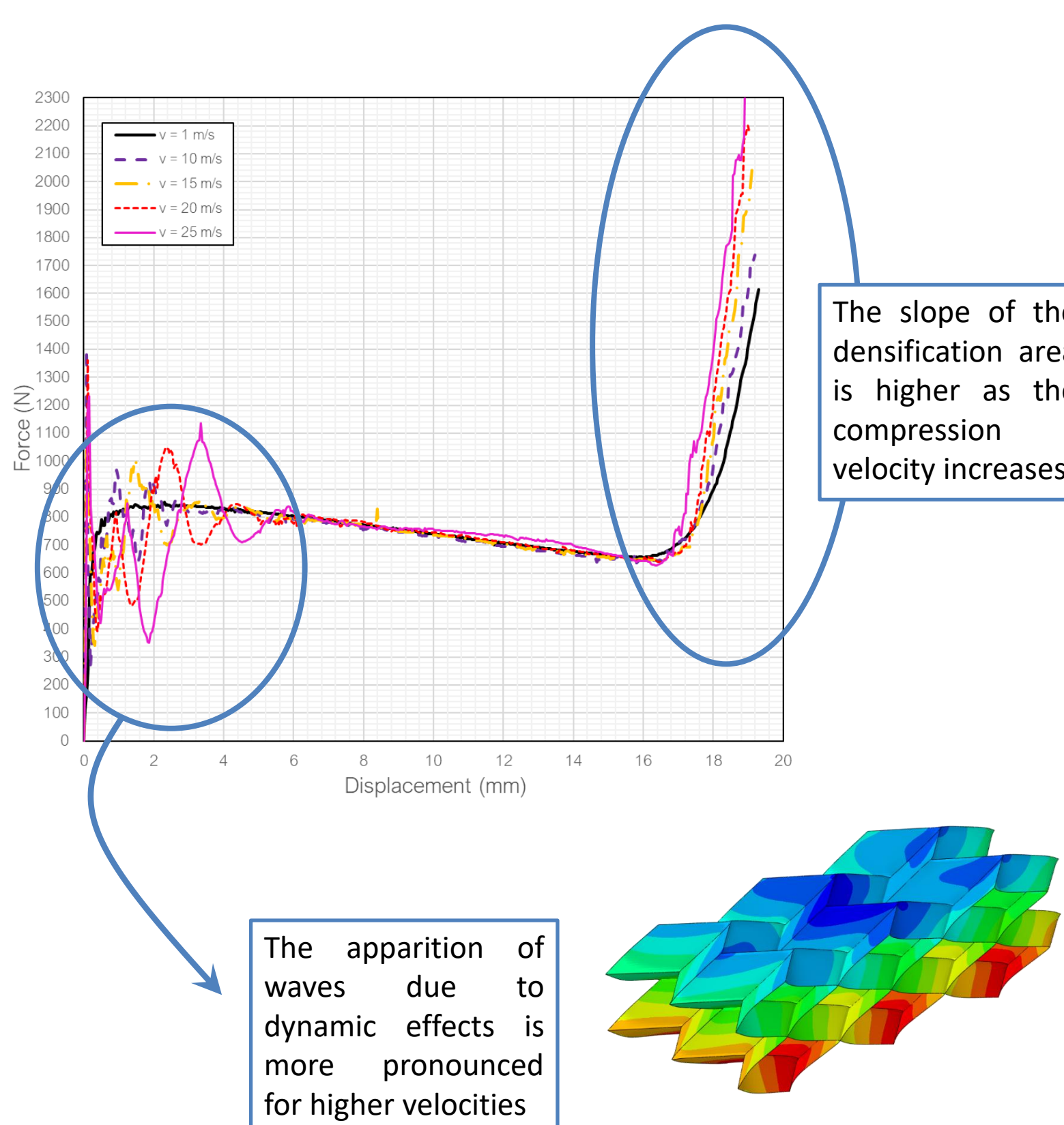
4.1. Effect of stacked sequence

Two deformation mechanisms occur: **unfolding** and **crushing** (associated with buckling phenomena in the panels). The occurrence of one or the other is governed by the **self-locking phenomenon**.

Applying compression perpendicular to the stacking direction results in **auxetic behavior** of the structure (negative Poisson's ratio). In this case, **there is hardly any difference between a homogeneous and a heterogeneous structure**.



4.2. Influence of the compression velocity



5. Concluding Remarks

- Using the Finite Element Method, a full 3-D numerical model of the compression tests in multi-layer metamaterial plate, has been implemented.
- The **numerical model has been validated** with results published in the literature, leading to a **relative error of about 3 %**.
- The morphological evolution of the structure during the compression process reproduce accurately the experimental observations.
- The **self-locking phenomenon** that occurs in heterogeneous metastructures determines the predominant deformation mechanism: **unfolding or crushing**.
- Energy absorption capacity** increases significantly in **heterogeneous structures**.
- Applying compression perpendicular to the stacking direction of the individual layers results in **auxetic behavior of the metastructure**. This behavior is not affected by the type of structure (homogeneous or heterogeneous).
- The slope of the densification area in the Force-Displacement curve is higher as the compression velocity increases.

References

- [1] Ma J., Song J., Chen Y. An origami-inspired structure with graded stiffness. International Journal of Mechanical Sciences 2018; 136:134-142.
- [2] Fossati M., Giglio M., Manes A. Fatigue crack propagation in a helicopter component subjected to impact damage. Defence Technology 2021; 17: 416-428.
- [3] Yu X., Zhou J., Liang H., Jiang Z., Wu L. Mechanical metamaterials associated with stiffness, rigidity and compressibility: A brief review. Progress in Materials Science 2018; 94:114-173.
- [4] Mousanezhad D., Haghpanah B., Ghosh R., Hamouda A.S., Nayeb-Hashemi H., Vaziri A. Elastic properties of chiral, anti-chiral, and hierarchical honeycombs: a simple energy-based approach. Theoretical and Applied Mechanics Letters 2016; 6:81-96.

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